

Int II End of Year Final Review

1. Filipe surveyed students at his school. He found that 78 students own a cell phone and 57 of those students own an mp3 player. There are 13 students that do not own a cell phone, but own an MP3 player. Nine students do not own either device. Construct a two-way table summarizing the data.

	MP3 Player	No MP3 Player	Total
Cell Phone	57, 0.81	21, 0.1	78
No Cell Phone	13, 0.19	9, 0.3	22
Total	70	30	100

2. Find the relative frequencies by column. Record them in the table. What is the relative frequency of the number of students with no cell phone to the total number of students surveyed?

$$\frac{22}{100} = 0.22$$

3. Order the following from least to greatest:

$$\sqrt{24}, 5.3, 5\frac{1}{4}, 5.\overline{25}$$

\downarrow \downarrow
 4.9 5.25

$$\sqrt{24}, 5\frac{1}{4}, 5.\overline{25}, 5.3$$

4. What is the definition of an irrational number? List 5 numbers that are irrational.

- a number that cannot be written as a fraction or
 - a non-repeating, nonterminating decimal $\pi, \sqrt{2}, \sqrt{7}, \sqrt[3]{9}, \sqrt[3]{20}$

5. Which 2 consecutive integers does $-\sqrt{80}$ lie between on the number line?

$$-\sqrt{80} = -8.9$$

-9 and -8

6. Evaluate $5(x^2 - y^3) + (y - x)^4$ for $x = -3$ and $y = 5$.

$$5((-3)^2 - 5^3) + (5 - (-3))^4$$

$$5(9 - 125) + (8)^4$$

$$5(-116) + 32$$

$$-580 + 32 = -548$$

7. Evaluate each expression for $x = -5$

$$5(-5)^4$$

$$5(625) = 3,125$$

$$(5x)^4 \quad (5 \cdot -5)^4$$

$$(-25)^4 = 390,625$$

$$5x^4$$

8. Simplify using exponent rules.

$$(6abc^2)^4(7a^2b^3c)^5$$

$$(6^4a^4b^4c^8)(7^5a^{10}b^{15}c^5)$$

$$6^47^5a^{14}b^{19}c^{13}$$

9. Solve: $\frac{x}{-4} + 7 = -3$

$$\frac{x}{-4} + 7 = -3$$

$$\frac{x}{-4} = -10$$

$$-4 \cdot \frac{x}{-4} = -10 \cdot -4$$

$$x = 40$$

10. Solve $6(x + 2) = 4x + 9 + 2x + 11$

$$6x + 12 = 4x + 9 + 2x + 11$$

$$6x + 12 = 6x + 20$$

$$-6x \quad -6x$$

$$12 \neq 20 \quad \text{NO solution}$$

11. Translate into an equation.

6 less than the quotient of a number and 5 is

13. $\frac{x}{5} - 6 = 13$

12. Write an equation to represent the following situation: Ryan has already made 24 cookies and bakes 12 more every hour. He needs 72 cookies total. How many hours does he need to keep baking cookies?

$$24 + 12h = 72$$

13. Solve $8(3a + 6) = 9(2a + 4)$

$$\begin{array}{r} 24a + 48 = 18a + 36 \\ -18a \quad -18a \\ \hline 6a + 48 = 36 \quad 6a = 84 \\ -48 \quad -48 \quad a = 14 \end{array}$$

14. Solve $8(c + 9) = 6(2c + 12) + 4c$

$$\begin{array}{r} 8c + 72 = 12c + 72 + 4c \\ -8c \quad -8c \\ \hline -72 = -72 \end{array}$$

All real numbers

15. Write and solve an equation: At the fair, Hunter bought 3 snacks and 10 ride tickets. Each ride ticket costs \$1.50 less than a snack. If he spends a total of \$24.00, what was the cost of each snack?

$x = \$3$

$$\begin{array}{l} 3x + 10(x - 1.50) = 24 \\ 3x + 10x - 15 = 24 \\ \quad +15 \quad +15 \\ \hline 13x = 39 \\ \quad 13 \quad 13 \\ \hline x = 3 \end{array}$$

16. Solve $8.0 + 5v + 6.3 = 4v + 2.3 + v$

$$\begin{array}{r} 5v + 1.7 = 5v + 2.3 \\ -5v \quad -5v \\ \hline 1.7 = 2.3 \end{array}$$

NO solution

17. What is the definition of a function?

each input has exactly one output

18. Draw a qualitative graph to represent the situation: Mary is hiking at a constant rate. She slows down for a while because she is tired. Then she stops to take a break. Then she continues hiking at her fastest speed yet.



19. Describe how to tell if a function is linear.

- if the graph is a straight line
- the rate of change is constant

20. Find the function value $f(-4)$ for $f(x) = 8 - 12x$

$$\begin{array}{l} f(-4) = 8 - 12(-4) \\ \quad \quad \quad 8 + 48 = 56 \end{array}$$

21. Create a table representing a linear

x	y
0	13
1	18
2	23
3	28

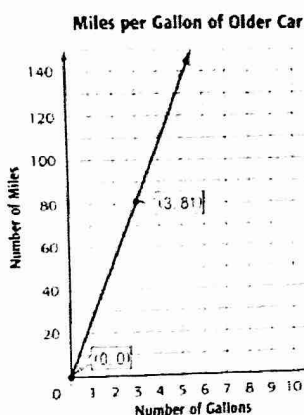
sample
answer

22. Find the slope of the line that passes between the two points.

$(-3, 7)$ and $(-6, -4)$

$$\frac{y_2 - y_1}{x_2 - x_1} = \frac{-4 - 7}{-6 - (-3)} = \frac{-11}{-3} = \frac{11}{3}$$

23. Find the slope of the line.



$$\frac{\Delta y}{\Delta x} = \frac{81 - 0}{3 - 0}$$

$$\frac{81}{3} = 27 \text{ mi/gal}$$

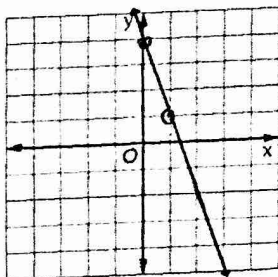
24. Find the slope from the table.

x	y
-2	5
-1	3
0	1
1	-1

$$\frac{-2}{1}$$

25. Write an equation for the line in slope-intercept form.

$$y = -3x + 4$$



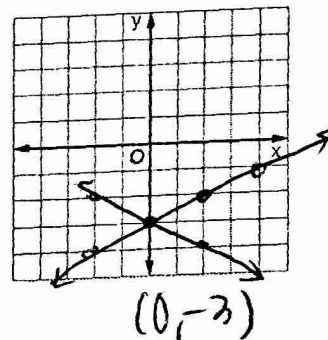
26. Find the solution to the system of linear equations.

$$y = \frac{1}{2}x - 3$$

$$2y + x = -6$$

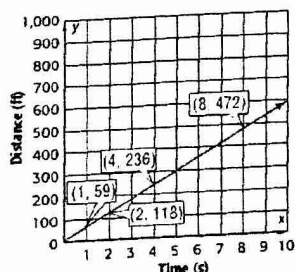
$$\frac{2y}{2} = \frac{-x - 6}{2}$$

$$y = -\frac{1}{2}x - 3$$



27. A zebra's main predator is a lion. Lions

can run at a speed of 53 feet per second over short distances. The graph at the right shows the speed of a zebra. Which animal has a faster speed and by how much?



Lion by
6 ft per sec

28. The function $m = 140h$, where m is the miles traveled in h hours, represents the speed of the first Japanese high speed train. The speed of a high speed train operating today in China is shown in the table.

Assume the relationship between the two quantities is linear. If you ride each train for 5 hours, how far will you travel on each?

Train Rate in China

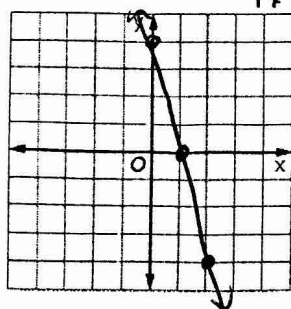
Hours	Miles
1	217
2	434
3	651

Japan.
 $m = 140(5)$

700
mi

China
 $m = 217(5)$
1085 mi

29. Graph the equation $y + 4x = 5$



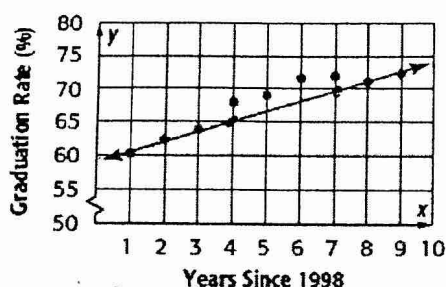
$$y = -4x + 5$$

30. The table shows how much money Ava has saved. Assume the relationship between the two quantities is linear. Write an equation to represent the situation.

Number of Months, x	Money Saved (\$), y
3	110
4	130
5	150
6	170

$$y = 20x + 90$$

31. The scatter plot shows the graduation rate of high school students. Write an equation for the line of best fit.



$$y = \frac{5}{3}x + 59$$

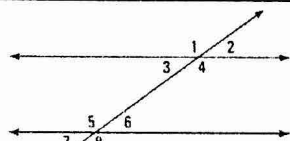
32. Use your equation to make a conjecture for the graduation rate in the year 2020. $2020 - 1998 = 22$

$$y = \left(\frac{5}{3}\right)(22) + 59$$

$$y = 36\frac{2}{3} + 59$$

$$y = 95\frac{2}{3}\%$$

33. List all sets of each type of angle.



Alternate interior: $\angle 3$ and $\angle 6$, $\angle 4$ and $\angle 5$
 Alternate exterior: $\angle 1$ and $\angle 8$ and $\angle 2$ and $\angle 7$
 Corresponding: $\angle 1$ and $\angle 5$, $\angle 2$ and $\angle 6$, $\angle 3$ and $\angle 7$, $\angle 4$ and $\angle 8$
 Supplementary: $\angle 1$ and $\angle 2$, $\angle 1$ and $\angle 3$, $\angle 4$ and $\angle 3$, $\angle 4$ and $\angle 2$, $\angle 5$ and $\angle 6$, $\angle 5$ and $\angle 7$, $\angle 6$ and $\angle 8$, $\angle 7$ and $\angle 8$
 (There are more Supplementary angles)

35. What is the sum of the interior angles of a triangle.

$$180^\circ$$

34. Use the figure from question 33. Find the value of x if $m\angle 3 = 10x - 20$ degrees and $m\angle 4 = 6x + 8$ degrees.

$$10x - 20 + 6x + 8 = 180$$

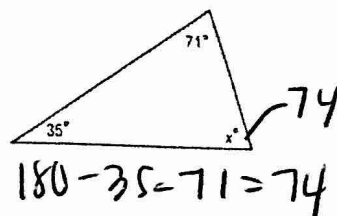
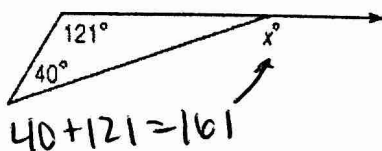
$$16x - 12 = 180$$

$$+12 +12$$

$$16x = 192$$

$$x = 12$$

36. Find the value of x in each figure below.



37. Find the sum of the interior angles of a dodecagon (12 sides).

$$(12-2)180$$


$$10(180)$$

$$1800^\circ$$

38. Find the measure of one exterior angle of a regular 14-gon.

$$\frac{360}{14} = 25.7^\circ$$

39. A right triangle has legs that measure 5 ft and 12 ft. What is the length of the hypotenuse?



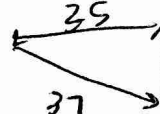
$$5^2 + 12^2 = x^2$$

$$25 + 144 = x^2$$

$$\sqrt{169} = \sqrt{x^2}$$

$$13 = x \quad \boxed{13 \text{ ft}}$$

40. Burke drives due North 12 miles and then due East 35 miles and then straight back to where he started. How far did he drive total?



$$12^2 + 35^2 = c^2$$

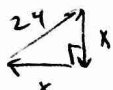
$$144 + 1225 = c^2$$

$$1369 = c^2$$

$$c = 37$$

$$\text{total} = 12 + 35 + 37 = \boxed{84 \text{ mi}}$$

41. Eliza usually drives straight to her friend Anna's house. Today, she drives the long way and goes x miles south and x miles west. If Anna's house is exactly 24 miles away, what is the value of x ? Round to the nearest tenth.




$$x^2 + x^2 = 24^2$$

$$\frac{2x^2}{2} = \frac{24^2}{2}$$

$$x^2 = \frac{24^2}{2}$$

$$x = \sqrt{\frac{24^2}{2}} = \sqrt{288} \approx 16.97 \approx 17.0$$

42. A right triangle has legs that measure $\sqrt{14}$ miles and $\sqrt{26}$ miles. What is the length of the hypotenuse?



$$(\sqrt{14})^2 + (\sqrt{26})^2 = c^2$$

$$14 + 26 = c^2$$

$$40 = c^2$$

$$c = \sqrt{40} \approx 6.32 \text{ mi}$$

43. Find the distance between the two points. Round to the nearest hundredth if necessary.

$(-9, -3)$ and $(5, -2)$

$$\sqrt{(5 - (-9))^2 + (-2 - (-3))^2}$$

$$\sqrt{14^2 + 1^2}$$

$$\sqrt{196 + 1} = \sqrt{197} \approx 14.03$$

44. On a map a park is located at $(12.325, 15.546)$ and the library is located at $(16.425, 18.575)$. How far is it from the park to the library? Round to the nearest thousandth.

$$\sqrt{(16.425 - 12.325)^2 + (18.575 - 15.546)^2}$$

$$\sqrt{4.1^2 + 3.029^2} = \sqrt{16.81 + 9.174841} \approx 5.098$$

45. Find the volume of a cylinder with a diameter of 12 feet and a height of 5 feet.

$$r = 6 \text{ ft}$$

$$V = (3.14)(6^2)(5)$$

$$V = 565.2 \text{ ft}^3$$

46. Find the volume of a cone with a radius of 4 cm and a height of 8 cm.

$$V = \frac{(3.14)(4^2)(8)}{3}$$

$$V = 133.97 \text{ cm}^3$$

47. What is the volume of a cylinder with a radius of 2.5 inches and a height of 3.75 inches.

$$V = (3.14)(2.5)^2(3.75)$$

$$73.59 \text{ in}^3$$

48. The volume of a cone is 294.375 cubic feet and the height is 5 feet. Find the radius of the cone.

$$294.375 = \frac{(3.14)(5)r^2}{3}$$

$$3 \cdot 294.375 = \frac{15.7}{3} r^2$$

$$883.125 = 5.23 r^2$$

$$\frac{883.125}{5.23} = r^2$$

$$168.85 = r^2$$

$$\sqrt{168.85} = r$$

$$12.99 \text{ ft} = r$$

49. Find the volume of a sphere with a radius of 14.5 inches.

$$V = \frac{4}{3}(3.14)(14.5)^3$$

$$V = 12,763.58 \text{ in}^3$$

50. Find the volume of a hemisphere with a diameter of 15 meters.

$$r = 7.5$$

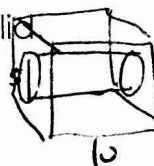
$$V = \frac{2}{3}(3.14)(7.5)^3$$

$$1766.25 \text{ m}^3$$

51. I have a sphere full of sand that has a radius of 4 in. Could I empty the sand into a cube that has a side length of 4? Explain.

NO, The sphere has a greater volume.
 Cube: $4^3 = 64 \text{ in}^3$
 Sphere: $\frac{4}{3}(3.14)(4^3) = 267.95 \text{ in}^3$

52. A cube with a side length of 10 cm has a cylindrical hole drilled out of the center. The diameter of the cylinder is 5 cm. Find the volume of the resulting solid.



$$\text{Cube} = 10^3 = 1000 \text{ cm}^3$$

$$\text{Cylinder} = (3.14)(5^2)(10) = 785 \text{ cm}^3$$

$$1000 - 785 = 215 \text{ cm}^3$$

53. Triangle ABC has vertices A(1, 2), B(2, 4), and C(4, 6). Give the coordinates after a reflection across the y-axis.

$$(-x, y)$$

$$A'(-1, 2) \quad B'(-2, 4) \quad C'(-4, 6)$$

54. Using triangle ABC from question 53 find the coordinates after a rotation of 90 degrees counter clockwise about the origin.

$$(-y, x)$$

$$A'(-2, 1) \quad B'(-4, 2) \quad C'(-6, 4)$$

55. Given the preimage and the image describe the transformation.

$$A(5, -3) \rightarrow A'(3, 5) \quad (-y, x)$$

rotate 270°
clockwise

56. Describe the translation using translation notation.

$$B(6, 2) \rightarrow B'(2, -3)$$

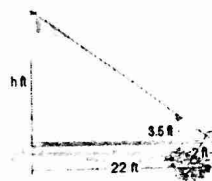
$$(x-4, y-5)$$

57. What transformations create congruent figures?

reflection
rotation
translation

58. How tall is the flagpole?

How tall is the flagpole?



$$\frac{h}{3.5} = \frac{22}{2}$$

$$2h = \frac{77}{2}$$

$$h = 38.5 \text{ ft}$$

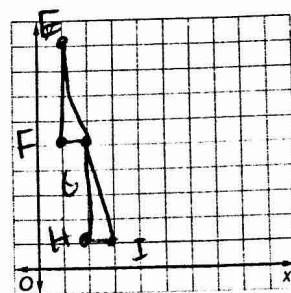
59. Which transformations create similar figures?

dilations

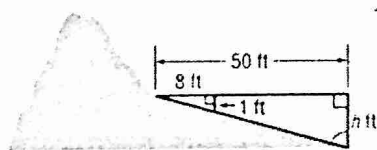
Graph each pair of similar triangles. Then write a proportion comparing the rise to the run for each of the similar slope triangles and find the numeric value.

60. $\triangle EFG$ with vertices $E(1,9)$, $F(1,5)$, and $G(2,5)$; $\triangle GHI$ with vertices $G(2,5)$, $H(2,1)$, and $I(3,1)$

$$\frac{EF}{FG} = \frac{GH}{HI} = 3$$



61. Find the depth of the water 50 feet from the shore?

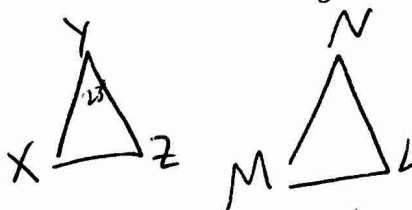


$$\frac{h}{1} = \frac{50}{8}$$

$$50 = \frac{8h}{8}$$

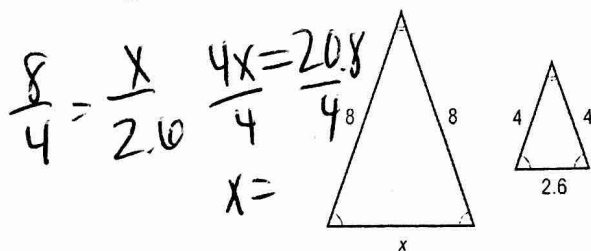
$$h = 6.25 \text{ ft}$$

62. Triangles XYZ and MNL are congruent if $m\angle XYZ = 23$ degrees. Find $m\angle MNL$.



23°

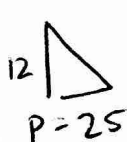
63. The triangles are similar. Find the length of the missing side.



$$\frac{8}{4} = \frac{x}{2.6} \quad \frac{4x}{4} = \frac{20.8}{4}$$

$$x =$$

64. Two triangles are similar. The smaller triangle has a height of 12 inches and a perimeter of 25 inches. The larger triangle has a height of 26 inches. Find the perimeter of the larger triangle.

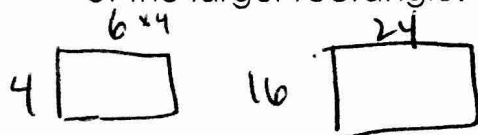


$$\frac{26}{12} = \frac{P}{25}$$

$$\frac{12P}{12} = \frac{650}{12}$$

$$P = 54.1\bar{6} \text{ in}$$

65. A rectangle has a side length of 4 inches and an area of 24 square inches. A larger similar rectangle has a side length of 16 inches. Find the area of the larger rectangle.



$$A = 24$$

$$384 \text{ in}^2$$

or

$$\frac{36}{12} = \frac{P}{25} \quad \frac{12P}{12} = \frac{900}{12} \quad P = 75 \text{ in}$$