

**Intermediate II  
Chapter 6 Review**

**6.1 (Translations)**

Remember: Translations are just SLIDING the image around the coordinate plane

Pre-image: original image (A, B, C)

Image: new image AFTER transformation of any kind (A', B', C')

IF you're moving LEFT OR RIGHT, this affects your X-COORDINATE.

IF you're moving UP OR DOWN, this affects your Y-COORDINATE.

TRANSLATION NOTATION: (change in all x-coordinates, change in all y-coordinates)

Example: Shift the pre-image left 3 and up 4:  $(x - 3, y + 4)$

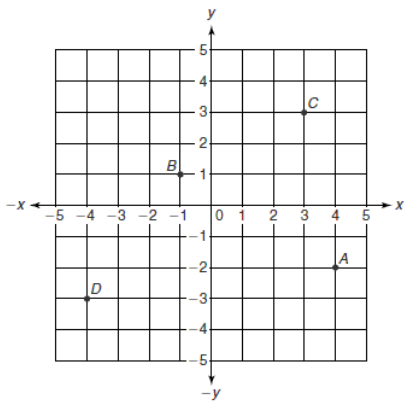
**Sample Problems:**

Write the following transformations in translation notation.

1. Shift 3 down and 4 to the right.
2. Shift 2 up and 6 to the left
3. Shift 4 down and 5 to the right.

4.  $A(3, -4) \rightarrow A'(5, 0)$

5.  $B(-4, -2) \rightarrow B'(-6, 2)$

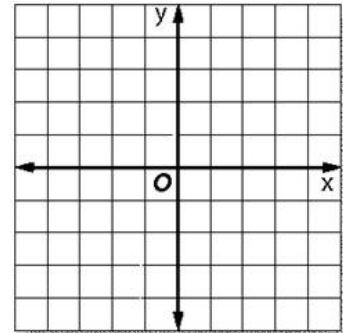


6. Translation notation from point D to point A:

7. Translation notation from point A to point B:

8. Translation notation from point C to point A:

9. Graph triangle A(-4, 0), B(-4, 3), and C(-1, 0) and its image after a translation of  $(x+2, y-4)$ .



10. Give the vertices of W(-1, -3), X(-1, 2), Y(2, -3), Z(2, 2) after a translation of 5 units up and 3 units to the right.

## 6.2 Reflections

REFLECTION: a mirror image that is CONGRUENT to the pre-image

Two lines of symmetry (this year ☺):

Reflection over the X-AXIS: x-coordinate stays the same; y-coordinate changes signs (same, -)

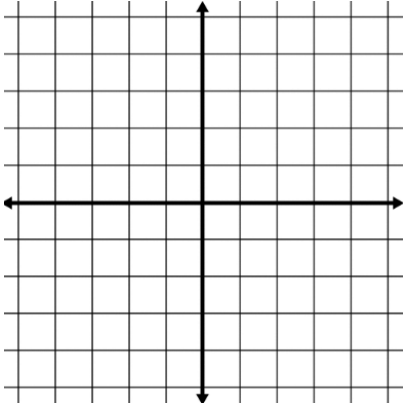
Reflection over the Y-AXIS: x-coordinate changes signs; y-coordinate stays the same (-, same)

### Sample Problems:

1. Graph the following triangle on both coordinate planes below.

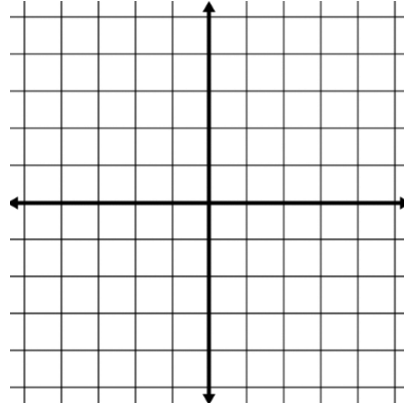
Triangle ABC has coordinates  $A(2,3)$   $B(3,1)$  and  $C(4,3)$ .

Graph triangle ABC's reflection over the x-axis. Write the new coordinates.



New coordinates:

Graph triangle ABC's reflection over the y-axis. Write the new coordinates.

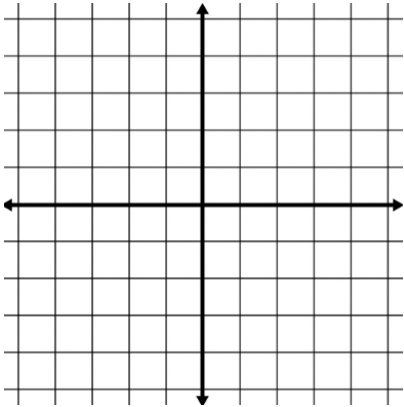


New coordinates:

2. Graph the following triangle on both coordinate planes below.

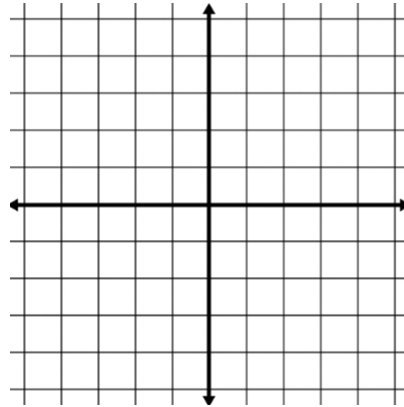
Triangle DEF has coordinates  $A(-2,-3)$   $B(-3,0)$  and  $C(2,5)$ .

Graph triangle DEF's reflection over the x-axis. Write the new coordinates.





New coordinates:

Graph triangle DEF's reflection over the y-axis. Write the new coordinates.

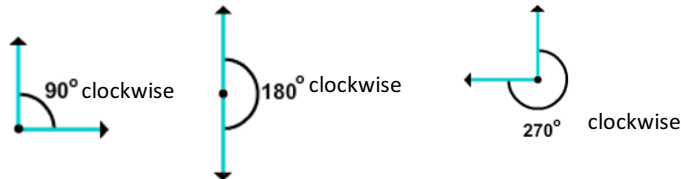


New coordinates:

## 6.3 Rotations

Rotations are clockwise (to the  right) or counter-clockwise  (to the left)

Degrees we use (this year ☺) are  $90^\circ$ ,  $180^\circ$ , and  $270^\circ$



\* $90^\circ$  clockwise is \_\_\_\_\_ counterclockwise,

$180^\circ$  clockwise is \_\_\_\_\_ counterclockwise,  $270^\circ$  clockwise is \_\_\_\_\_ counterclockwise

There are two kinds of rotations:

- \* Rotation about the origin
- \* Rotation about a fixed point (not the origin)

### Rotations about the ORIGIN

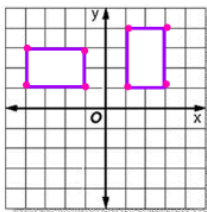
$90^\circ$

Clock-wise:

$$(x, y) \rightarrow ( \quad , \quad )$$

Counter Clock-wise:

$$(x, y) \rightarrow ( \quad , \quad )$$



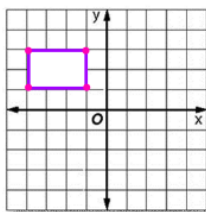
$180^\circ$

Clock-wise:

$$(x, y) \rightarrow ( \quad , \quad )$$

Counter Clock-wise:

$$(x, y) \rightarrow ( \quad , \quad )$$



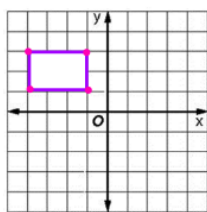
$270^\circ$

Clock-wise:

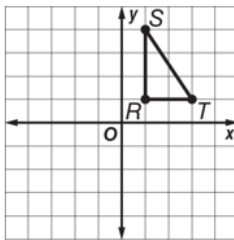
$$(x, y) \rightarrow ( \quad , \quad )$$

Counter Clock-wise:

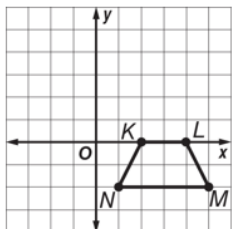
$$(x, y) \rightarrow ( \quad , \quad )$$



Triangle  $RST$  has vertices  $R(1, 1)$ ,  $S(1, 4)$ , and  $T(3, 1)$ . Graph the figure and its rotated image after a clockwise rotation of  $180^\circ$  about the origin. Then give the coordinates of the vertices for triangle  $R'S'T'$ .

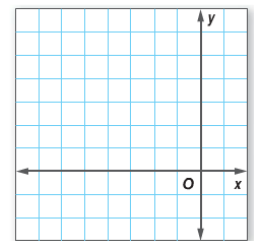


Quadrilateral  $KLMN$  has vertices  $K(2, 0)$ ,  $L(4, 0)$ ,  $M(5, -2)$ , and  $N(1, -2)$ . Graph the figure and its rotated image after a counterclockwise rotation of  $90^\circ$  about the origin. Then give the coordinates of the vertices for quadrilateral  $K'L'M'N'$ .

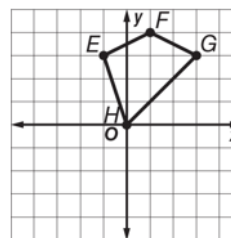


### Rotations about a Fixed Point

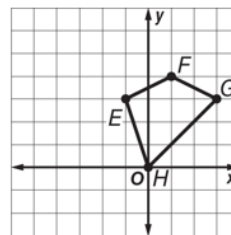
Rectangle  $ABCD$  with vertices  $A(-7, 4)$ ,  $B(-7, 1)$ ,  $C(-2, 1)$ , and  $D(-2, 4)$  represents the bed in Jackson's room. Graph the figure and its image after a clockwise rotation of  $90^\circ$  about vertex  $C$ . Then give the coordinates of the vertices for rectangle  $A'B'C'D'$ .



$90^\circ$  clockwise about vertex  $H$



$180^\circ$  counterclockwise about vertex  $E$



## 6.4 Dilations

Multiply each  $x$  value and each  $y$  value by the scale factor ( $k$ )

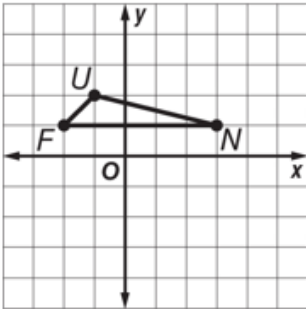
$k > 1$ , then the dilation is an enlargement (get's bigger)

$k < 1$ , then the dilation is a reduction (get's smaller)

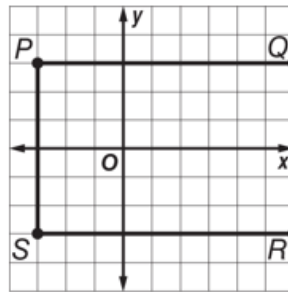
$k = 1$ , then the figure stays the same size

Sample Problems:

$$F(-2, 1), U(-1, 2), N(3, 1); k = 2$$



$$P(-3, 3), Q(6, 3), R(6, -3), S(-3, -3); k = \frac{1}{3}$$



David built a model of a regulation basketball court. His model measured approximately 3.75 feet long by 2 feet wide. The dimensions of a regulation court are 94 feet long by 50 feet wide. What is the scale factor David used to build his model?

## Review of Solving Equations

$$-3x - 4 = 4x + 10$$

$$2(m + 3) - 5 = 5 + 2m$$

$$5(z + 1) + 14 = 19 - 2z + 7z$$